The Crystal Structure of Ru₃Be₁₇*

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 $\operatorname{Ru}_3\operatorname{Be}_{17}$ is body-centered cubic with a = 11.337 Å; there are eight formula units in the unit cell and the space group is Im3. A feature of the structure which is unusual for an intermetallic beryllide is the occurrence of a hole of radius 2.81 Å around the origin of the unit cell. Powder patterns show a corresponding isostructural osmium beryllide with a = 11.342 Å.

Introduction

Powder diffraction patterns of Ru-Be preparations showed a body-centered cubic phase of approximate composition RuBe₆. Single crystals of this phase were subsequently made. The determination of its crystal structure established its correct stoichiometry as Ru_3Be_{17} .

Experimental

Samples of Ru₃Be₁₇ were prepared from -50 mesh 99.9% pure Ru powder and -200 mesh 99% pure Be powder. The main impurity in the Be was oxygen. The powders were mixed in an atomic ratio of one Ru to six Be to make up 1 g. of sample. This mixture was reacted in a dense BeO crucible at 1480 °C. for 15 min. under $\frac{1}{2}$ atmosphere argon. An inductively heated Ta crucible was used as the furnace. The sample showed evidence of reaction, but not of melting. Two higher heatings were made in attempts to melt the sample. Melting was not indicated at 1530 °C., but did occur at 1635 °C. The resultant sample was crushed and single crystals were selected for the structural study.

Powder diffraction patterns taken with Cu $K\alpha$ radiation ($\lambda K\alpha_1 = 1.54050$ Å, $\lambda K\alpha_2 = 1.54434$ Å) show that the material is body-centered cubic with

$$a = 11.337 \pm 0.005$$
 Å.

The first 17 lines of this pattern are listed in Table 1. Powder patterns show a corresponding isostructural osmium beryllide with $a=11\cdot342$ Å. Oscillation and Weissenberg photographs of a single crystal of Ru₃Be₁₇ showed Laue symmetry Im3. The possible space groups, consistent with the diffraction effects, are I23, I2₁3, and Im3. The choice of the centrosymmetric space group, Im3, was ultimately confirmed by the structure determination.

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Table 1. Powder pattern of Ru_3Be_{17} Photographed with $CuK\alpha$ radiation, $\lambda = 1.5418$ Å.Intensities estimated visually

			•		
d	hkl	Ι	d	hkl	Ι
8·1 Å	110	10	$2 \cdot 525$ Å	420	25
5.64	200	30	$2 \cdot 408$	332	25
4.60	211	15	$2 \cdot 308$	422	10
3 ·99	220	45	2.219	$\begin{cases} 510 \\ 431 \end{cases}$	30
3.56	310	100	2.062	2521	50
3.25	222	65	1.937	∫ 530 \ 433	100
3 ·01	321	100	1.883	$\left\{\begin{array}{c} 442\\600\end{array}\right.$	45
2.82	$\left\{\begin{array}{c} 411\\ 330 \end{array}\right.$	25	1.832	$\left\{\begin{array}{c} 611\\532\end{array}\right.$	100

The intensities from an irregularly shaped single crystal of approximate dimensions $0.04 \times 0.06 \times 0.08$ mm. were measured with Mo $K\alpha$ radiation on a General Electric XRD-5 X-ray spectrometer equipped with a single crystal orienter. The stationary crystal-stationary counter technique was used, and 40-sec. counts were taken at the calculated settings of all reflections with $2\theta \leq 60^{\circ}$. Background corrections were obtained from a plot of intensity versus θ made with the crystal out of reflecting position. The intensities of 506 reflections, of which 13 were not observable above background, were measured.

Structure determination

Preparations of intermetallic beryllides are generally microcrystalline. Establishing their stoichiometries by chemical analysis is complicated by the necessity for proving that the material is single phase and by the possibility that some of these compounds have extended homogeneity ranges. The solution of the stoichiometry problem is usually based upon a combination of the structure determination and the assumption of the additivity of elemental volumes (e.g., Zalkin, Sands & Krikorian, 1959). In the present case, the volume of the unit cell is 1457 Å³, and the volume of 24 Ru atoms plus 140 Be atoms obtained from the elements (13.57 Å³/Ru, 8.105 Å³/Be) is 1460

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Table 2. Observed and calculated structure factors, F_o and F_c , respectively

Asterisks denote unobserved reflection

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Table 3. Atomic parameters of Ru₃Be₁₇

Atom	Position	x	y	z	B
Ru	24(q)	0	0.1879 ± 0.0001	0.3014 ± 0.0001	0.2 Å^2
Be,	48(h)	0.2010 ± 0.0011	0.1140 ± 0.0011	0.3434 ± 0.0011	1.1
Be	24(q)	$\overline{0}$	0.2305 ± 0.0015	0.0914 ± 0.0015	0.9
Be	24(g)	0	0.4055 ± 0.0012	0.3488 ± 0.0012	0.2
Be	16(f)	0.1645 ± 0.0010	0.1645 ± 0.0010	0.1645 ± 0.0010	0.9
Be ₅	$12(\epsilon)$	0.1956 ± 0.0017	$\overline{0}$	2	0.2
Be_6	12(d)	0.4065 ± 0.0023	0	0	$1 \cdot 2$

Å³, suggesting the composition Ru_6Be_{35} with four of these formula units per unit cell.

The 24 Ru atoms were found, by interpretation of the three-dimensional Patterson function, to occupy positions 24(g) of space group Im3: body-centering $\pm (0, y, \pm z; z, 0, \pm y; y, \pm z, 0)$ (International Tables for X-ray Crystallography, 1952), with y = 0.19, z = 0.31. The relationship, $y + z = \frac{1}{2}$, which these unrefined parameters obey, has been observed for the metalloid atoms in the isostructural compounds CoAs₃ (Oftedal, 1928), CoSb₃ (Rosenqvist, 1953), RhSb₃ (Zhuravlev & Zhdanov, 1956), and IrAs₃ and IrSb₃ (Kjekshus & Pedersen, 1961). A consequence of this relationship is that no new vectors would be added to the vector set if an atom were placed at the origin. However, the magnitudes of the vectors would be changed, and quantitative consideration of the heights of the Patterson peaks shows that, in this case, there is no heavy atom at the origin and the above interpretation of the Patterson is, in fact, unique if the space group is Im₃.

The contributions of the Ru atoms to the structure factors were computed, and the resulting signs were applied to the observed structure factors which were then used in calculating the three-dimensional Fourier synthesis. The positions of 136 beryllium atoms were obtained from this Fourier map. In terms of space group Im3 they are:

48 Be ₁ in $48(h)$:	$\pm (x, \pm y, \pm z; z, \pm x, \pm y; y, \pm z, \pm x)$
	+ body-centering,
	with $x = 0.20$, $y = 0.11$, $z = 0.34$,
24 Be_2 in $24(g)$	with $y = 0.23$, $z = 0.09$,
24 Be ₃ in $24(g)$	with $y = 0.40, z = 0.35,$
16 Be ₄ in $16(f)$:	$\pm (x, \pm x, \pm x) + \text{body-centering},$
	with $x=0.16$,
12 Be_5 in $12(e)$:	$\pm (x, 0, \frac{1}{2}; \frac{1}{2}, x, 0; 0, \frac{1}{2}, x) + \text{body-}$
	centering, with $x = 0.20$,
12 Be_6 in $12(d)$:	+(x, 0, 0; 0, x, 0; 0, 0, x) + body

centering, with x = 0.40.

The volume calculation predicted the presence of 140 Be atoms per unit cell. The 136 Be atoms found leave holes of radius 2.81 Å around the 2(a) positions $(0, 0, 0; \frac{1}{2}, \frac{1}{2}, \frac{1}{2})$. However, four atoms cannot be added to the structure without destroying the cubic symmetry. The possibility of placing a third of a Be atom in each of the 12(d) positions, with x=0.1, was tested in the course of the least squares refinements. The temperature factors of these fractional atoms

increased rapidly, reaching 8.7 Å² after two cycles. Similar results occurred when Be atoms were placed in the 2(a) positions. Furthermore, the energy required to transfer a Be atom from the lattice to a hole of 2.81 Å radius would be of the order of the energy necessary to vaporize the atom. Finally, a difference Fourier was computed after refinement of the 136 Be and 24 Ru atoms. The largest peak on this difference map corresponded to about 1.5 electrons near a Be₄ atom; the next largest peaks amounted to only about 0.5 electron. The most negative region was at the origin. Since there are no other holes of sufficient size to accommodate additional atoms, the conclusion was reached that there are only 136 Be atoms per unit cell, and the formula of this phase is Ru₃Be₁₇.

The Ru₃Be₁₇ parameters were refined on an IBM 709 using the least squares program of Busing & Levy (1959). Individual isotropic temperature factors for each atom were included in the refinements. Constant weighting factors were applied. The atomic scattering factors used were those of Thomas & Umeda (1957) for Ru, and Ibers (1957) for Be. The final reliability factor, $R = \Sigma |F_o - F_c|/\Sigma |F_o|$, was 0.052. Omitting the unobserved reflections, R was 0.049. The standard error of fit, $[\Sigma | F_o - F_c|^2/(m-n)]^{\frac{1}{2}}$, was 4.83 (m = 506)was the number of observations, n=20 was the number of parameters being refined). The observed and calculated structure factors are listed in Table 2. The refined parameters are given in Table 3. The standard errors of the parameters were computed by Busing & Levy's program.

Discussion

The nearest neighbor interatomic distances of Ru_3Be_{17} are listed in Table 4. The standard deviations of these distances were computed by the method of Cruickshank & Robertson (1953).

The point symmetry at a Ru atom is $C_{s}-m$. Its neighbors include four Be₁, two Be₂, three Be₃, two Be₄, and one Be₅ arranged at the vertices of a truncated tetrahedron. Four additional neighbors, consisting of two Be₁ atoms at 2.38 Å, one Be₂ atom, and one Be₆ atom, lie on the axes of the hexagonal faces of the truncated tetrahedron. This configuration about the heavy atom (Fig. 1) has also been observed in NbBe₂ and NbBe₃ (Sands, Zalkin & Krikorian, 1959) and in ReBe₂₂ (Sands, Johnson, Zalkin, Krikorian & Kromholtz, 1962).

Table 4. Interatomic distances in Ru₃Be₁₇

Ru-2 Be ₁	2.474 ± 0.012	Å Be ₃ –2 R	$2 \cdot 528 \pm 0.006$ Å
-2 Be	2.379 ± 0.013	–1 R	u 2.525 ± 0.013
-2 Be	2.464 ± 0.013	-2 B	$e_1 2.188 \pm 0.015$
-1 Be,	2.429 ± 0.017	-2 B	$e_1 2.230 \pm 0.017$
2 Be	2.501 ± 0.009	-1 B	$e_3 2.143 \pm 0.027$
-1 Be ₃	$2 \cdot 525 \pm 0.013$	-1 B	$e_5 2.062 \pm 0.017$
-2 Be ₃	$2 \cdot 528 \pm 0.006$	-1 B	$e_5 2.041 \pm 0.021$
-2 Be	2.441 ± 0.018	-2 H	$e_6 2.282 \pm 0.017$
-1 Be ₅	2.610 ± 0.010		•
-1 Be ₆	$2 \cdot 442 \pm 0 \cdot 013$	Be ₄ –3 R	$2 \cdot 441 \pm 0.018$
, i i i i i i i i i i i i i i i i i i i		-3 B	$e_1 2 \cdot 148 \pm 0 \cdot 017$
Be ₁ -1 Ru	2.474 ± 0.012	-3 E	$e_2 2 \cdot 174 \pm 0.020$
–1 Ru	$2 \cdot 379 \pm 0 \cdot 013$		
–l Ru	2.464 ± 0.013	Be_{5} –2 R	2.610 ± 0.010
-2 Be_1	$2 \cdot 195 \pm 0 \cdot 021$	-4 H	$e_1 2.197 \pm 0.013$
-1 Be ₁	2.585 ± 0.025	-2 B	$e_3 2.062 \pm 0.017$
$-1 \operatorname{Be}_2$	$2 \cdot 202 \pm 0 \cdot 019$	-2 B	$e_3 2.041 \pm 0.021$
-1 Be ₃	2.230 ± 0.017	-2 E	$e_6 2.457 \pm 0.021$
$-1 \operatorname{Be}_3$	2.188 ± 0.015		
-1 Be_4	2.048 ± 0.017	Be_{6} –2 F	$10 2.442 \pm 0.013$
$-1 \operatorname{Be}_5$	$2 \cdot 197 \pm 0 \cdot 013$	-4 E	$e_1 2.716 \pm 0.014$
-1 Be ₆	2.716 ± 0.014	-2 H	$6e_2 2 \cdot 249 \pm 0 \cdot 029$
		-4 E	$e_3 2 \cdot 282 \pm 0 \cdot 017$
Be ₂ –I Ru	2.429 ± 0.017	-2 F	$3e_5 2.457 \pm 0.021$
-2 Ru	2.501 ± 0.009	-1 E	$Be_6 2.118 \pm 0.052$
-2 Be ₁	$2 \cdot 202 \pm 0 \cdot 019$		
-1 Be ₂	$2 \cdot 073 \pm 0 \cdot 033$		
-2 Be ₄	2.174 ± 0.020		
-1 Be ₆	2.249 ± 0.029		
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Fig. 1. Nearest neighbors of Ru.

Each of the Be₁, Be₂, Be₃, and Be₄ atoms has six beryllium and three ruthenium neighbors arranged at the vertices of two octahedra sharing a face. The vertices of the shared face are in each case occupied by the ruthenium atoms. The Be₃ atoms have three additional neighbors, consisting of one Be₅ and two Be₆ atoms, forming a triangle centered about 1.7 Å from Be₃ along the common axis of the octahedra. The Be₁ environment also includes this extra triangle, in this case consisting of one Be₁, one Be₅, and one Be₆ atom, but the distances from the central Be₁ atom to these atoms are 2.72 Å, 2.20 Å, and 2.59 Å, respectively.

The Be₅ atoms occupy positions of point symmetry C_{2v} -mm. Each Be₅ is surrounded by a prism with quadrilateral bases. The sequence of atoms at the vertices of each base is Be₁-Be₆-Be₁-Be₃. The axis of the prism is bisected by a trapezoid whose vertices are occupied by the sequence Be₃-Be₃-Ru-Ru.



Fig. 2. Environment of two Be₆ atoms.

The Be₆ atoms occur in pairs. The environment of such a pair is shown in Fig. 2. The Be₁ atoms in this picture serve only to complete the cage, the Be₆-Be₁ distance (2.72 Å) being too large to be considered an interatomic contact. The Be₆-Be₅ distance is 2.46 Å.

The hole at the origin is bounded by 12 Be₂ atoms at a distance of 2.81 Å. This hole also appears in the CoAs₃ structure, where it is bounded by 12 metalloid atoms at a distance varying from 3.1 Å in CoAs₃ to 3.5 Å in IrSb₃. The electron-to-atom ratios for the Ru₃Be₁₇ and CoAs₃ structures are 2.60 and 2.67, respectively, based on Pauling's valences (1960) of 6 for Ru, 2 for Be, 6 for Co, and 1.56 for As.

We wish to thank Mr Vernon G. Silveira for the powder photography. We are also indebted to Dr William J. Ramsey for helpful discussions.

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Refinement of the Crystal Structure of Co₉S₈

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The structure of Co_9S_8 has been refined in space group $O_h^5 - Fm3m$ by the least-squares technique applied to selected single-crystal data. The lattice constant of Co_9S_8 is $9\cdot928 \pm 0\cdot001$ Å and there are four Co_9S_8 in the unit cell. There are two kinds of cobalt atoms in the structure: one is surrounded by a regular octahedron of sulfur atoms with Co-S distance, $2\cdot39 \pm 0\cdot03$ Å; the other is surrounded by a tetrahedron of S atoms, one Co-S distance being $2\cdot13 \pm 0\cdot02$ Å, and the other three being $2\cdot21 \pm 0\cdot02$ Å. Each of the cobalt atoms with tetrahedral sulfur coordination is also linked to three similarly coordinated cobalt atoms at a distance of $2\cdot50 \pm 0\cdot02$ Å which is essentially the Co-Co distance in the elementary cobalts. Some comparison is made with the Rh-S coordination in Rh₁₇S₁₅ and it is tentatively concluded that an anomaly exists in the apparent sizes of the octahedrally coordinated metal atoms.

Introduction

The crystal structure of Co_9S_8 was solved by Lindqvist, Lundqvist & Westgren (1936) from powder data. In their paper, Lindqvist *et al.* point out that several authors had proposed erroneous formulas for this compound or its isomorph pentlandite, ((Ni, Fe)₉S₈). Also Alsén (1925), assuming a formula of (Ni, Fe)₅ for pentlandite, had proposed an apparently erroneous structure.

As was pointed out in a recent paper on the structure of $Pd_{17}Se_{15}$ (Geller, 1962*a*), the interest in Co_9S_8 resulted from the possibility of a close relationship of its structure to that of the isostructural $Pd_{17}Se_{15}$ and $Rh_{17}S_{15}$ erystals. This was particularly so because of the reported (Juza *et al.*, 1935) formula, Rh_9S_8 , for the latter compound. Because of some difficulty with the solution of the structures of $Pd_{17}Se_{15}$ and $Rh_{17}S_{15}$, it was decided to check the Co_9S_8 structure with single-crystal data. The single-crystal material used in this analysis was very kindly given to us by Dr J. R. Stubbles^{*}; it had resulted from his investigations on self-diffusion in Co_9S_8 .

In our study of the single-crystal data from Co_9S_8 , concluded that the structure proposed by Lindqvist

et al. was essentially correct. The refinement, however, gives a substantially different viewpoint on the Co–S interatomic distances.

Experimental

A slightly imperfect sphere of average diameter 0.28 mm. was made from the single-crystal material with the Bond (1951) sphere grinder. The crystal was aligned along [100] as rotation axis and a set of Weissenberg photographs* taken with Mo $K\alpha$ radiation, for which the absorption coefficient, $\mu = 164.0$ cm.⁻¹, $\mu R = 2.3$. A set of precession-camera photographs was also taken with Mo $K\alpha$ radiation and [100] as precession axis. However only hk0 and hk1 intensities from the Weissenberg photographs (50 and 24 hr. exposures respectively) were estimated visually, by comparison with a calibrated intensity strip.

The diffraction symmetry of the crystal is m3mwith reflections hkl present only when h+k and k+lare even. There are no further systematic absences. Thus the probable space groups are: O_h^5-Fm3m , $T_q^2-F\bar{4}3m$ or O^3-F432 .

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^{*} Customarily, when using Mo $K\alpha$ radiation, the author uses a three film pack with sheets of Cu foil interleaved resulting in a film:film intensity ratio of approximately 4:1.